

Southfields Primary School



Calculations A guide for parents Year 3 and 4

Addition – Year 3

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

Addition - Year 3

Missing number problems using a range of equations as in Year 1 and 2 with appropriate, larger numbers.

Partition into tens and ones

Partition both numbers and recombine.

Count on by partitioning the second number only e.g.

$$\begin{aligned} 247 + 125 &= 247 + 100 + 20 + 5 \\ &= 347 + 20 + 5 \\ &= 367 + 5 \\ &= 372 \end{aligned}$$

Children need to be secure adding multiples of 100 and 10 to any three-digit number including those that are not multiples of 10. Number lines can still be used.

Towards a written method

Introduce expanded column addition modelled with place value containers (Dienes could be used for those who need a less abstract representation)

200	40	7
100	20	5
300	60	12
$= 372$		

$$\begin{array}{r} 247 \\ +125 \\ \hline 12 \\ 60 \\ \hline 300 \\ 372 \end{array}$$

Leading to children understanding the exchange between tens and ones.



Some children may begin to use a formal columnar algorithm, initially introduced alongside the expanded method. The formal method should be seen as a more streamlined version of the expanded method, not a new method.

$$\begin{array}{r} 247 \\ +125 \\ \hline 372 \\ 1 \end{array}$$

Addition - Year 3



$$\begin{array}{l} 213 + 4 = \\ \swarrow \quad \searrow \\ 210 \quad 3 \end{array} \qquad \begin{array}{l} 3 + 4 = 7 \\ 210 + 7 = 217 \end{array}$$

Add the ones, then the tens and then the hundreds



	Hundreds	Tens	Ones
	4	3	2
+	3	2	1
	7	5	3

$$432 + 321 = 753$$

Addition – Year 4

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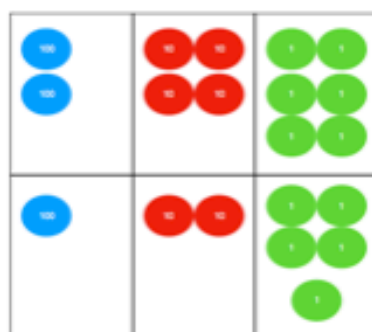
Addition - Year 4

Missing number/digit problems:

Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving.

Written methods (progressing to 4-digits)

Expanded column addition modelled with place value counters, progressing to calculations with 4-digit numbers.



$$\begin{array}{r} 200 + 40 + 6 \\ 100 + 20 + 5 \\ \hline 300 + 60 + 11 = 371 \end{array}$$

$$\begin{array}{r} 246 \\ + 125 \\ \hline 11 \\ 60 \\ 300 \\ \hline 371 \end{array}$$

Compact written method

Extend numbers with at least four digits.



$$\begin{array}{r} 2634 \\ + 4517 \\ \hline 7151 \\ 11 \end{array}$$

Children should be able to make the choice of reverting to expanded methods if experiencing any difficulty.

Extend to up to two places of decimals (same number of decimal places) and adding several numbers (with different numbers of digits).

$$\begin{array}{r} 72.8 \\ + 54.6 \\ \hline 127.4 \\ 11 \end{array}$$

Subtraction - Year 3

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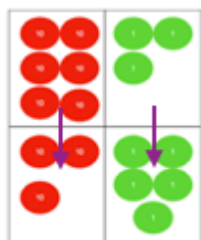
Subtraction - Year 3

Missing number problems e.g. $\square = 43 - 27$; $145 - \square = 138$; $274 - 30 = \square$; $245 - \square = 195$; $532 - 200 = \square$

Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving (see Y1 and Y2). Children should make choices about whether to use complementary addition or counting back, depending on the numbers involved.

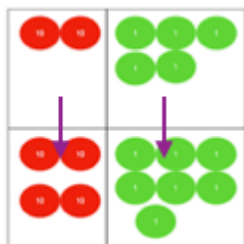
Written methods (progressing to 3-digits)

Introduce expanded column subtraction with no decomposition, modelled with place value counters (Dienes could be used for those who need a less abstract representation)



$$\begin{array}{r} 90 \ 8 \\ - 30 \ 5 \\ \hline 60 \ 3 \end{array}$$

For some children this will lead to exchanging, modelled using place value counters (or Dienes).



$$\begin{array}{r} 60 \ 1 \\ 70 \ 2 \\ - 40 \ 7 \\ \hline 20 \ 5 \end{array}$$

A number line and expanded column method may be compared next to each other.

Some children may begin to use a formal columnar algorithm, initially introduced alongside the expanded method. The formal method should be seen as a more streamlined version of the expanded method, not as a new method.

Subtraction - Year 3



$$\begin{array}{l} 8 - 4 = 4 \\ 50 + 4 = 54 \end{array}$$

Hundreds	Tens	Ones
9	7	5
-	7	2
2	5	2

H	T	O
8	7	5
-	7	2
8	0	5

Cubes can be used
Link to the bar model

Subtraction - Year 4

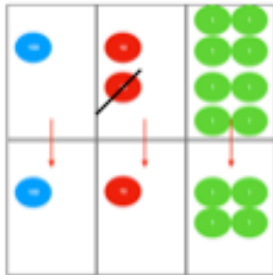
Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

Subtraction - Year 4

Missing number/digit problems: $456 + \square = 710$;
 $1\square7 + 6 = 200$; $60 + 99 + \square = 340$; $200 - 90 - 80 = \square$;
 $225 - \square = 150$; $\square - 25 = 67$; $3450 - 1000 = \square$;
 $\square - 2000 = 900$

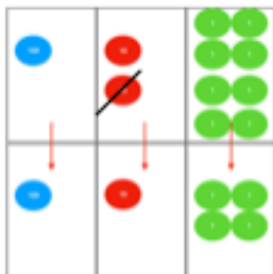
Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving.

Written methods (progressing to 4-digits) expanded column subtraction with decomposition, modelled with place value counters, progressing to calculations with 4-digit numbers.



$$\begin{array}{r} 20 1 \\ 200 30 2 \\ - 100 10 4 \\ \hline 100 10 8 \end{array}$$

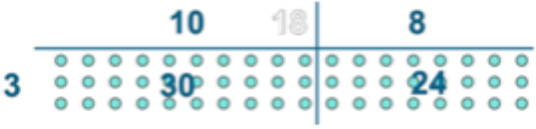
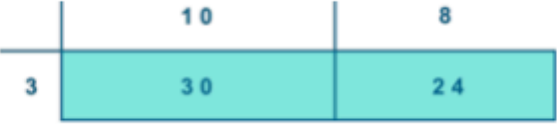


If understanding of the expanded method is secure, children will move on to the formal method of decomposition, which again can be initially modelled with place value counters.



$$\begin{array}{r} 21 \\ 232 \\ -114 \\ \hline 118 \end{array}$$

Multiplication – Year 3

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Multiplication - Year 3	Multiplication - Year 3
<p>Missing number problems Continue with a range of equations as in Year 2 but with appropriate numbers, Continue using the number line</p> <p>Mental methods Doubling 2-digit numbers using partitioning</p> <p>Demonstrating multiplication on a number line - jumping in larger groups of amounts</p> <p>$13 \times 4 = 10 \text{ groups } 4 + 3 \text{ groups of } 4$</p> <p>Written methods (progressing to 2-digits x 1-digit)</p> <p>Developing written methods using understanding of visual images</p>  <p>Develop onto the grid method</p>  <p>Give children opportunities for children to explore this and deepen understanding using Dienes apparatus and place value counters</p>	<p>$2 \times 4 = 8$</p>  <p>Ones 2 <u>x 4</u> 8</p> <p>Move onto $20 \times 4 =$</p>  <p>Tens Ones 2 0 <u>x 4</u> 8 0</p> <p>$23 \times 2 = 46$</p> <p>Tens Ones 2 3 <u>x 2</u> 6 6 4 0</p> <p>Tens Ones 2 3 <u>x 2</u> 6 6 4 0</p> <p>Tens Ones 2 3 <u>x 2</u> 6 6 4 0</p> <p>Tens Ones 2 3 <u>x 2</u> 6 6 4 0</p>

Multiplication – Year 4

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

Multiplication - Year 4

Continue with a range of equations as in Year 2 but with appropriate numbers. Also include equations with missing digits

$$2 \times 5 = 160$$

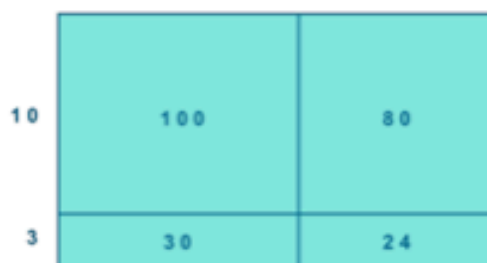
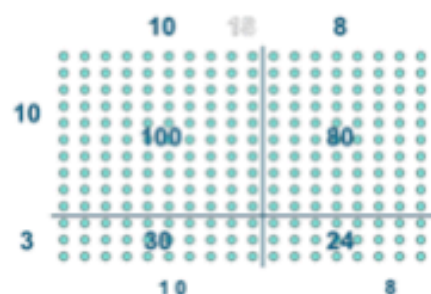
Mental methods

Counting in multiples of 6, 7, 9, 25 and 1000, and in steps of 1/100

Solving practical problems where children need to scale up. Relate to known number facts (e.g. how tall would a 25cm sunflower be if it grew 6 times taller?)

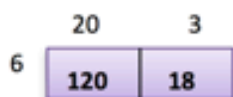
Written methods (progressing to 3-digit x 2-digit)

Children to embed and deepen their understanding of the grid method to multiply up 2-digit x 2-digit. Ensure this is still linked back to their understanding of arrays and place value counters.



$$\begin{array}{r} 23 \\ \times 6 \\ \hline 18 \\ + 120 \\ \hline 138 \end{array}$$

$$23 \times 6 =$$



$$\begin{array}{l} 20 \times 6 \quad 3 \times 6 \\ 23 \times 6 = 120 + 18 \\ = 138 \end{array}$$

Division and fractions – Year 3

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

Division - Year 3

\div = signs and missing numbers

Continue using a range of equations as in Year 2 but with appropriate numbers.

Grouping

How many 6's are in 30?

$30 \div 6$ can be modelled as:



Becoming more efficient using a number line

Children need to be able to partition the dividend in different ways.

$48 \div 4 = 12$



Remainders

$49 \div 4 = 12r1$



Sharing - 49 shared between 4. How many left over?

Grouping - how many 4s make 49? How many are left over?

Place value counters can be used to support children apply their knowledge of grouping.

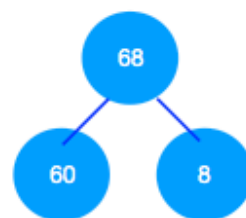
For example:

$60 \div 10 =$ How many groups of 10 in 60?

$600 \div 100 =$ How many groups of 100 in 600?

Division - Year 3

$68 \div 2 =$



6 tens $\div 2 = 30$



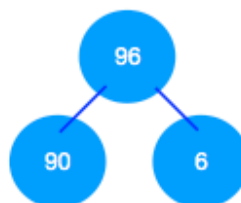
8 ones $\div 2 = 4$



$68 \div 2 = 30 + 4 = 34$

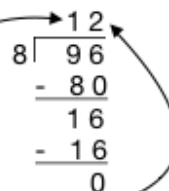


$96 \div 8 = 12$



8 tens $\div 8 = 1$ ten

16 ones $\div 8 = 2$ ones



Division and fractions – Year 4

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

Division - Year 4

= signs and missing numbers

Continue using a range of equations as in year 3 but with appropriate numbers.

Sharing, grouping and using a number line

Children will continue to explore division as sharing and grouping, and to represent calculations on a number line until they have a secure understanding. Children should progress in their use of written division calculations:

- using tables facts with which they are fluent

- experiencing a logical progression in the numbers they use, for example:

1. Dividend just over 10x the divisor, e.g. $84 \div 7$

2. Dividend just over 10x the divisor when the divisor is a teen number, e.g. $173 \div 15$ (learning sensible strategies for calculations such as $102 \div 17$)

3. Dividend over x100 the divisor, e.g. $840 \div 7$

4. Dividend over x20 the divisor, e.g. $168 \div 7$

e.g. $840 \div 7 = 120$

Jottings

$7 \times 100 = 700$

$7 \times 10 = 70$

$7 \times 20 = 140$

All of the above stages should include calculations with remainders as well as without.

Remainders should be interpreted according to the context (i.e. rounded up or down to relate to the answer of the problem).

100 groups

20 groups

0

700

840

Formal written methods

Formal short division should only be introduced once children have a good understanding of division, its links with multiplication and the idea of 'chunking up' to find a target number (see use of number lines above)

Short division to be modelled for understanding using place value counters as shown below. Calculations with 2 and 3-digit dividends, e.g. fig 1



$$\begin{array}{r} 34 \\ 2 \overline{) 68} \\ \underline{- 6} \\ 8 \\ \underline{- 8} \\ 0 \end{array}$$

6 tens \div 2

8 ones \div 2

$68 \div 2 = 34$

$75 \div 6 =$

$$\begin{array}{r} 12 \\ 6 \overline{) 75} \\ \underline{- 6} \\ 15 \\ \underline{- 12} \\ 3 \text{ remainder} \end{array}$$

6 tens \div 6

12 ones \div 6

$75 \div 6 = 12 \text{ r } 3$